

SIGNIFICANCE TESTING

CHEM 25 | SDSU

DIFFERENT RESULTS

Two students (A & B) have made measurements of samples taken from the same population.

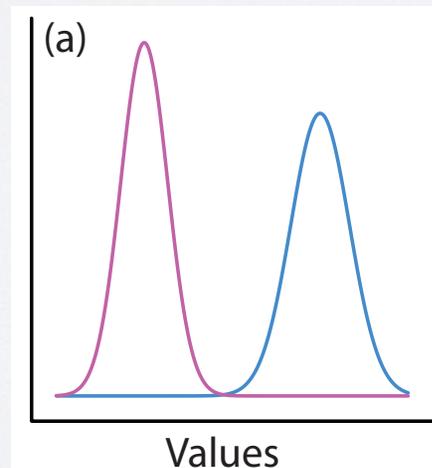
Determine the 95% confidence interval for each of their sample means.

Student A

14.555 to 14.746

Student B

14.331 to 14.518



Trials	Student A	Student B
1	14.602	14.408
2	14.782	14.517
3	14.668	14.322
4	14.534	14.477
5	14.721	14.398
6	14.596	
Average	14.6505	14.4244
Std. Dev.	0.091	0.075

TESTING DIFFERENT RESULTS

- The question raised by the results of Students A & B is whether or not the difference in their values was due to **indeterminate errors** or not.
- To determine this a **null hypothesis** (H_0) and **alternative hypothesis** (H_A) must be tested.
- The null hypothesis proposes that the difference can be sufficiently explained by indeterminate errors.
- The alternative hypothesis proposes that the difference are too great to be attributed to indeterminate errors.

USING THE TTEST

- The t test is used as a null hypothesis test; that the reported mean represents the true value.
- The test compares t_{exp} to $t_{(\alpha, \nu)}$, where α is the desired confidence level and ν are the degrees of freedom for the sample.
- If $t_{\text{exp}} > t_{(\alpha, \nu)}$ the difference cannot be explained by indeterminate errors, and we **reject the null hypothesis**.
- If $t_{\text{exp}} \leq t_{(\alpha, \nu)}$ the difference can be explained by indeterminate errors, and we **accept the null hypothesis**.

$$\mu = \bar{X} \pm \frac{(t_{\text{exp}})s}{\sqrt{n}}$$
$$t_{\text{exp}} = \frac{|\mu - \bar{X}| \sqrt{n}}{s}$$

Table 4.15 Values of t for a 95% Confidence Interval

Degrees of Freedom	t	Degrees of Freedom	t
1	12.706	12	2.179
2	4.303	14	2.145
3	3.181	16	2.120
4	2.776	18	2.101
5	2.571	20	2.086
6	2.447	30	2.042
7	2.365	40	2.021
8	2.306	60	2.000
9	2.262	100	1.984
10	2.228	∞	1.960

SAMPLE PROBLEM

If student A and B were both measuring a solution that had a concentration of 14.512 do either of the students' measurements agree with this value at the 90% confidence level?

Values of t for...		
...a confidence interval of:	90%	95%
...an α value of:	0.10	0.05
Degrees of Freedom		
1	6.314	12.706
2	2.920	4.303
3	2.353	3.182
4	2.132	2.776
5	2.015	2.571
6	1.943	2.447
7	1.895	2.365
8	1.860	2.306

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